



Toward Efficient Community Detection on Time-Varying Attributed Graphs

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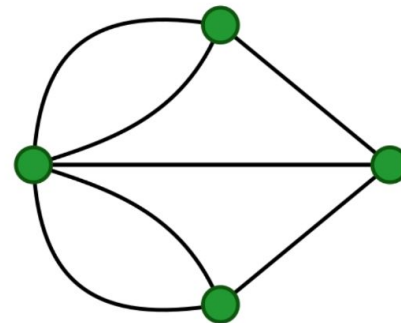
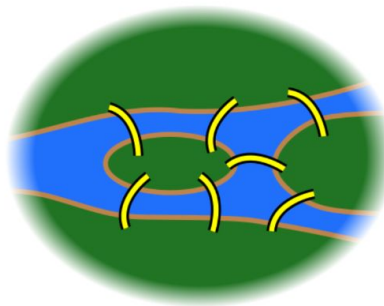
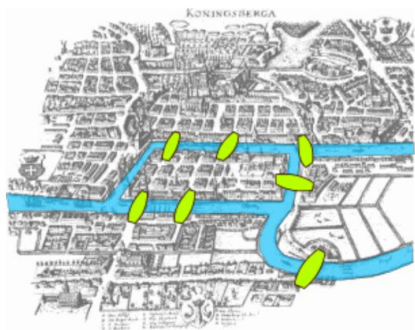
² National Research Council (ISTI-CNR)



1. Background

The problem and the science

- Many real-world systems can be modeled and studied as **networks** (or **graphs**).
- Elements are **nodes**, connections are **edges** – *often* mathematically constructed as **matrices**.

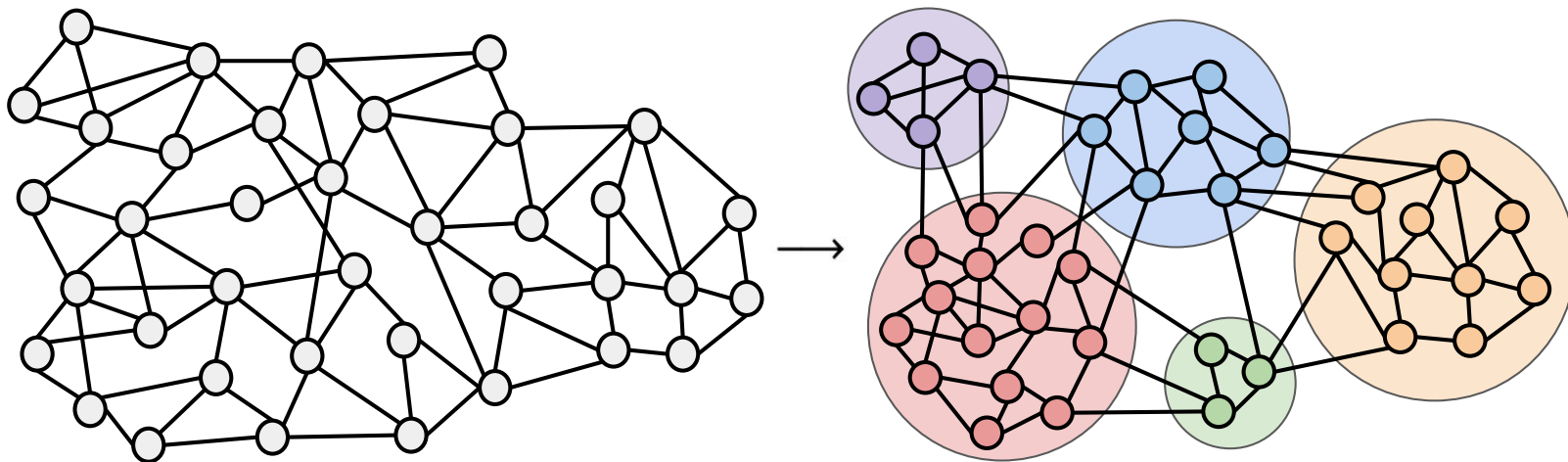


- But the systems we observe are rarely fixed (*static*) in time; instead, they *change* or *evolve*.
- A **temporal network** can be modeled as a **dynamic graph** – with *time-varying* nodes and edges.

1. Background

The problem and the science

- Our problem: how can we efficiently cluster nodes (*detect communities*) in a graph...

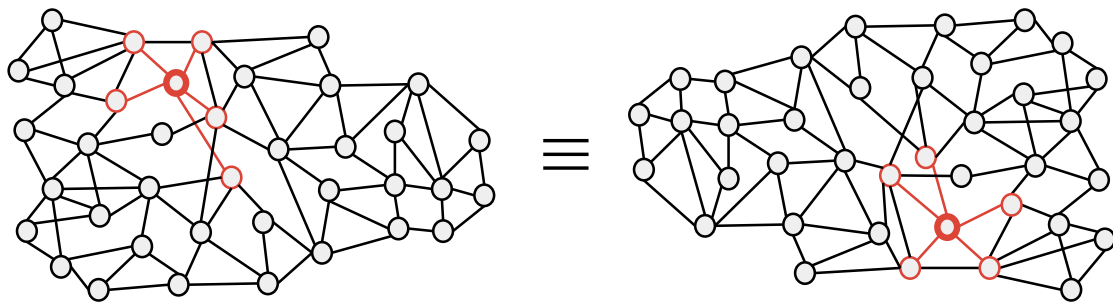


- ...when the graph changes over time and is associated (*attributed*) with additional metadata?

1. Background

The problem and the science

- Machine learning (ML) models are very good in approximating (*learning from*) lots of data.
- But classical ML models can not learn from relational (*non-Euclidean*) datasets directly...



- ...unless first *mapped* to a real-dimensional (*Euclidean*) space – the sort of space *we live in*.
- In the last ten years, a new kind of neural network has emerged that can learn from graphs.

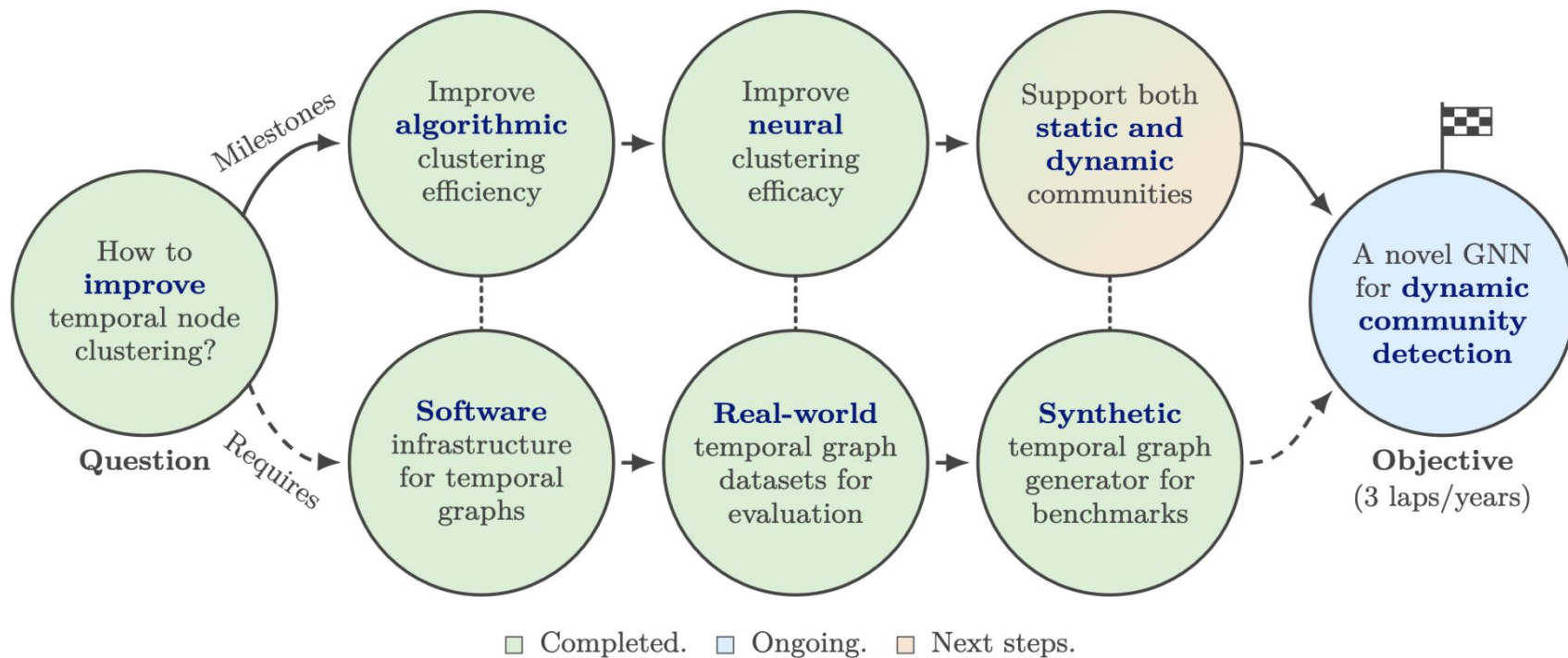
1. Background

The problem and the science

- How can we efficiently cluster nodes (*detect communities*) in an attributed temporal graph?
- State of the art: node clustering is performed with **algorithms** or **neural** models for graphs.
 - **Algorithms**: spectral clustering, heuristic optimization, statistical inference...
 - **Neural models**: graph neural networks (GNNs), which learn directly on graph-based structures.
- Methods from both approaches have been adapted from static to dynamic settings.
- But another question may be raised: when are **neural** models better than **algorithms** for the task?

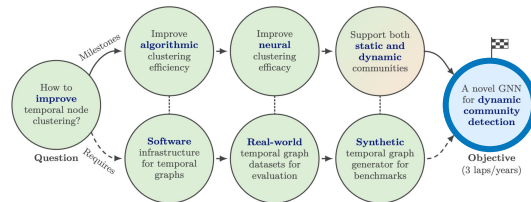
2. Schematic

Research trajectory



3. Contributions

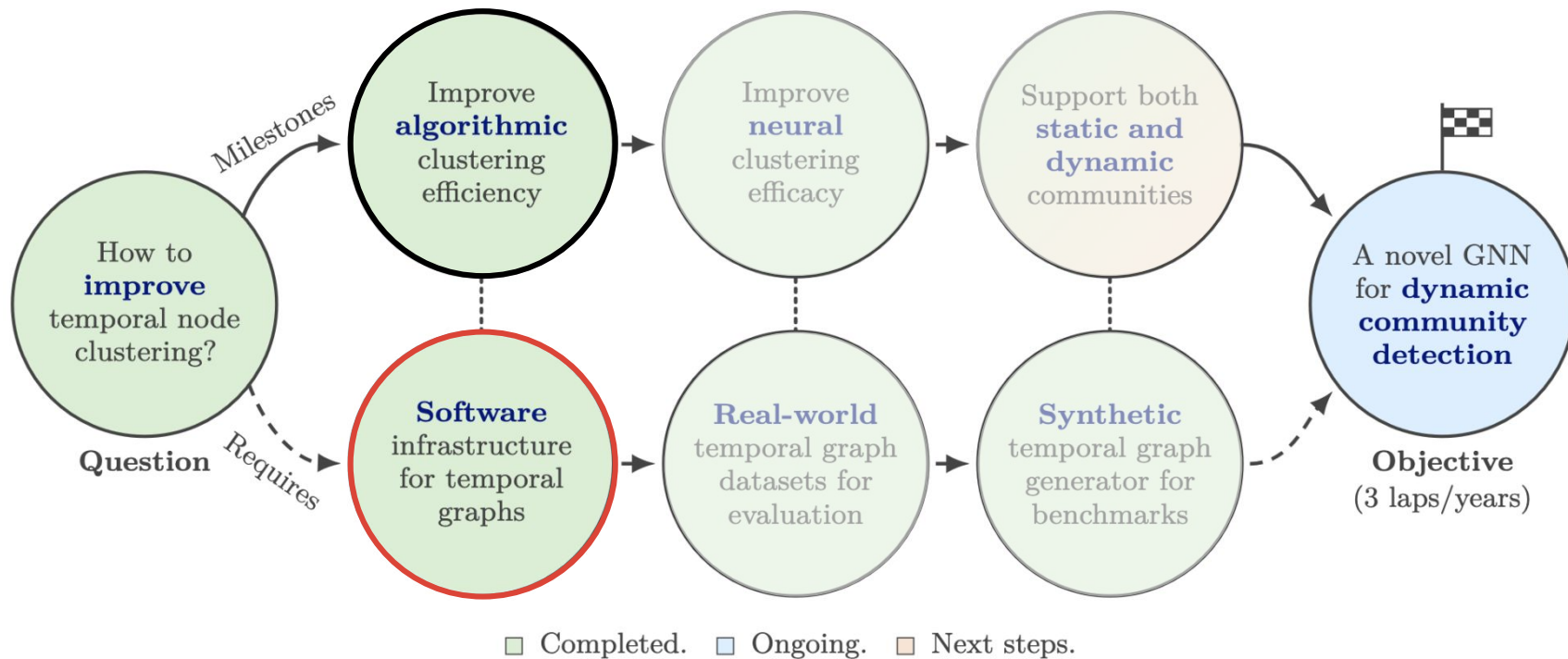
Requirements → Milestones



- Following this **research plan**, our contributions are threefold:
 - Improving algorithmic clustering efficiency (*scalability*)
 - Improving neural clustering efficacy (*performance accuracy*)
 - Supporting static and dynamic community detection (*in temporal graphs*)
- Altogether, they answer the **central research problem**, as well as the *underlying question*:
 - How to improve temporal node clustering?
 - When are neural models better than algorithms for the task?

3.1. Improve algorithmic clustering efficiency

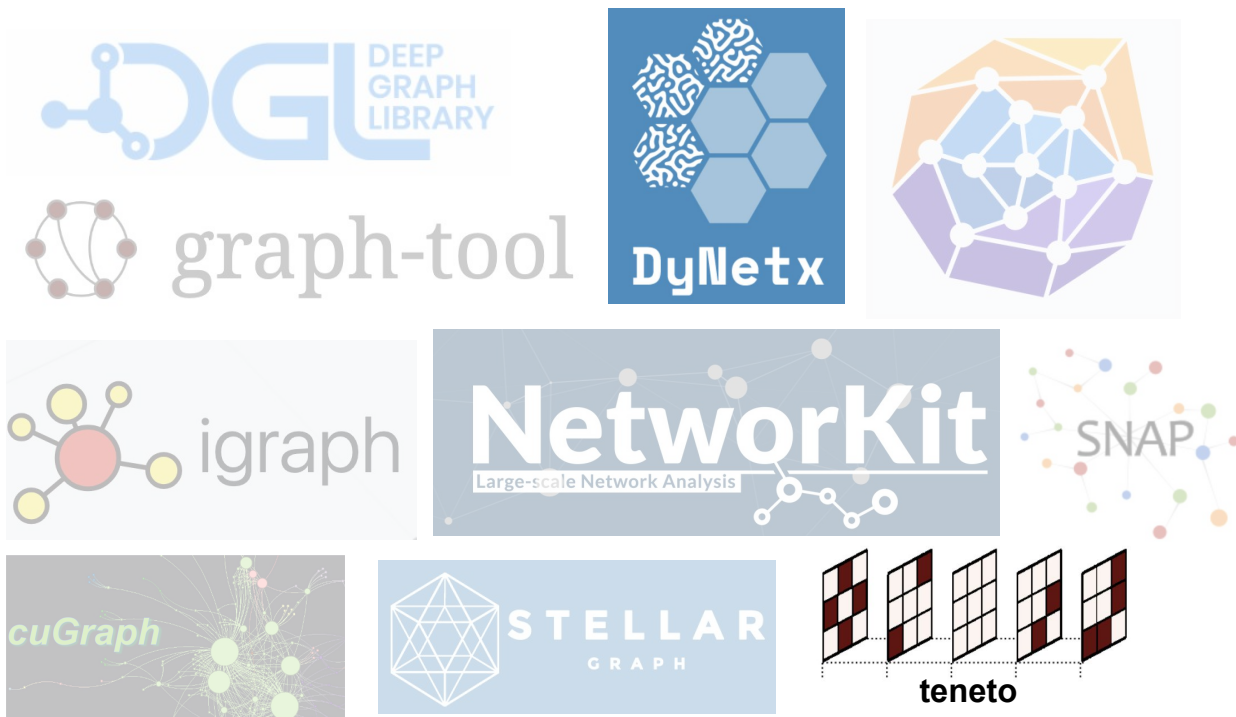
Requires: Software infrastructure for temporal graphs



3.1. Improve algorithmic clustering efficiency

Requires: Software infrastructure for temporal graphs

- At the start of this research, there was **no maintained software ecosystem** for temporal graphs.



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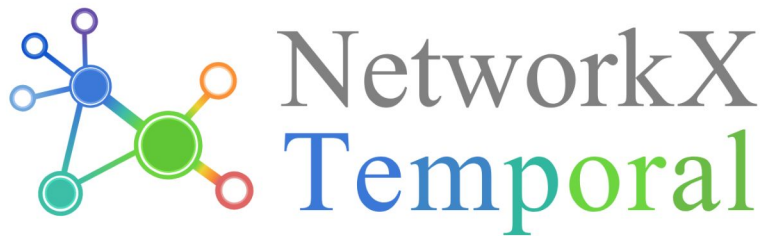
- At the start of this research, there was **no maintained software ecosystem** for temporal graphs.

Library	$\mathcal{G}$	Parameter	Description
cuGraph [119]		'cugraph'	Graph suite from NVIDIA RAPIDS.
CuPy [121]		'cupy'	Sparse GPU array representation.
Deep Graph Library [186]		'dgl'	Deep learning on graphs.
DyNetX [150]	✓	'dynetx'	Dynamic network analysis.
graph-tool [133]		'graph_tool'	High-performance graph operations.
igraph [28]		'igraph'	General-purpose network analysis.
NetworkKit [167]		'networkkit'	Scalable graph algorithms.
NumPy [71]		'numpy'	Dense vector representations.
PyTorch Geometric [40]		'torch_geometric'	Deep learning on graphs.
SciPy [183]		'scipy'	Sparse matrix representations.
SNAP [91]		'snap'	Large-scale network analysis.
StellarGraph [31]		'stellargraph'	Machine learning on graphs.
Teneto [175]	✓	'teneto'	Temporal network analysis.

3.1. Improve algorithmic clustering efficiency

Requires: Software infrastructure for temporal graphs

- The answer became **building** a new one, while **integrating** all other software shown before.



NetworkX-Temporal is a Python package for the creation, manipulation, and analysis of the structure and dynamics of temporal graphs — extending NetworkX with support for time-varying relational data.

Install from PyPI:

```
$ pip install networkx-temporal
```

 networkx-temporal.org

3.1. Improve algorithmic clustering efficiency

Requires: Software infrastructure for temporal graphs

- Open source and freely distributed (3-clause BSD license), the library includes functions for:
 - Easy snapshot slicing

```
>>> import networkx_temporal as tx
>>>
>>> TG = tx.temporal_graph() # TG = tx.TemporalMultiGraph()
>>>
>>> TG.add_edge("a", "b", time=0)
>>> TG.add_edge("c", "b", time=1)
>>> TG.add_edge("d", "c", time=2)
>>> TG.add_edge("d", "e", time=2)
>>> TG.add_edge("a", "c", time=2)
>>> TG.add_edge("f", "e", time=3)
>>> TG.add_edge("f", "a", time=3)
>>> TG.add_edge("f", "b", time=3)
>>>
>>> TG = TG.slice(attr="time")
>>>
>>> print(TG)
```

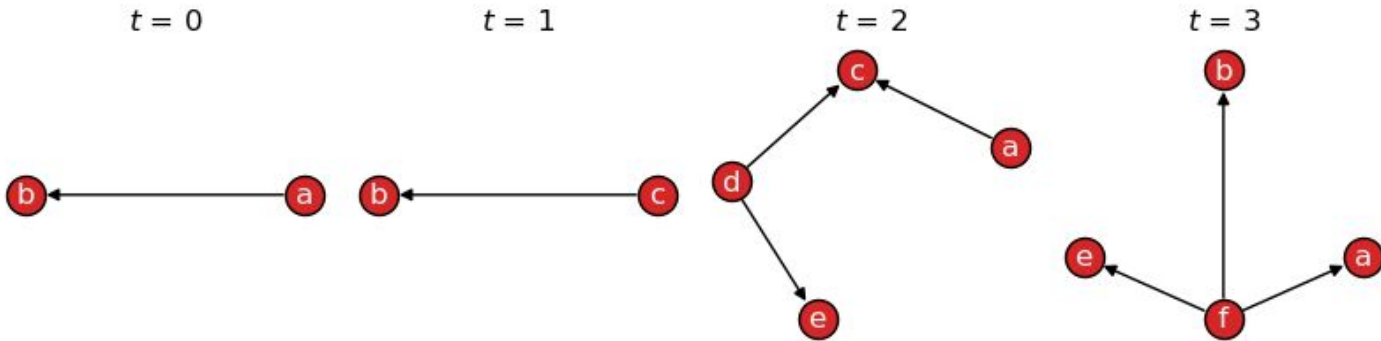
TemporalMultiGraph (t=4) with 6 nodes and 8 edges

3.1. Improve algorithmic clustering efficiency

Requires: Software infrastructure for temporal graphs

- Open source and freely distributed (3-clause BSD license), the library includes functions for:
 - Easy snapshot slicing
 - Drawing functions

```
>>> tx.draw(TG, layout="kamada_kawai", figsize=(8, 2))
```



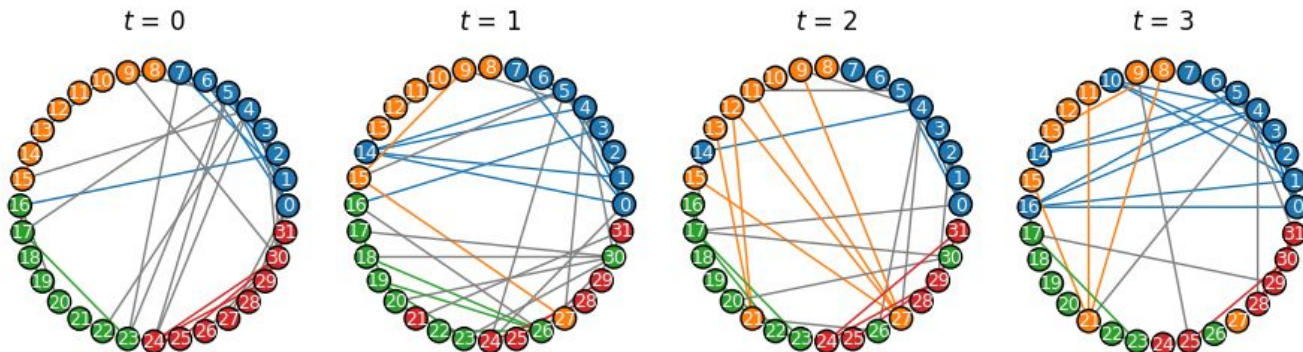
3.1. Improve algorithmic

Requires: Software infrastructure for temporal graph

- Open source and freely distributed (3-clause license)
- Easy snapshot slicing
- Drawing functions
- Data loaders/generators

```
>>> import networkx_temporal as tx
>>>
>>> n = 8           # Nodes per community.
>>> k = 4           # Number of communities.
>>> t = 4           # Number of temporal snapshots.
>>> p = 0.8         # Within-community edge probability.
>>> eta = 0.9       # Stability of community memberships.
>>> alpha = 2       # Exponent for degree distribution (Zipf).
>>>
>>> B = tx.generate_block_matrix(k, p)
>>> z = tx.generate_community_vector(n, k)
>>> d = tx.generate_degree_vector([n]*k, max_degree=n, alpha=alpha, seed=0)
>>> tau = tx.generate_transition_matrix(k, eta)
>>>
>>> TG = tx.generators.dynamic_sbm(
>>>     B=B, z=z, d=d, t=t,
>>>     transition_matrix=tau,
>>>     fix_transition_prob=False,
>>>     seed=0
>>> )
>>> print(TG)
```

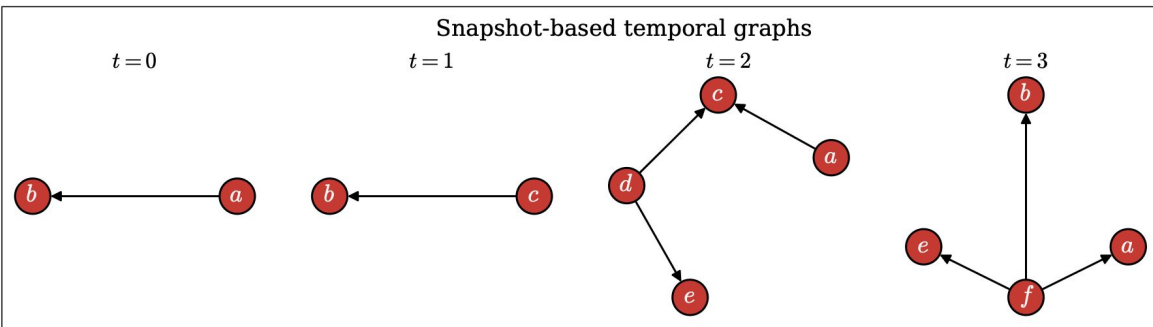
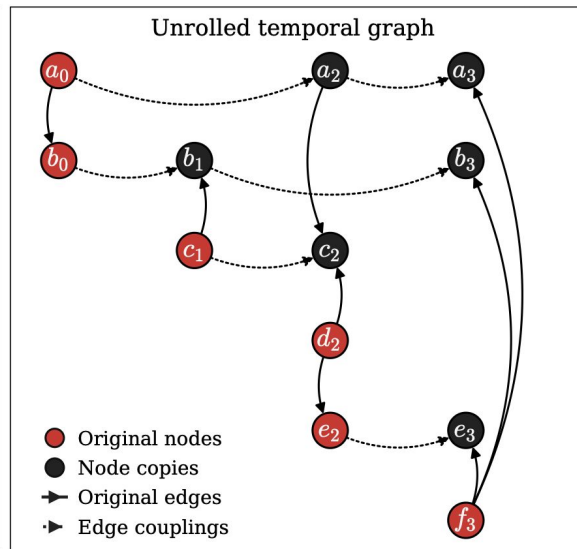
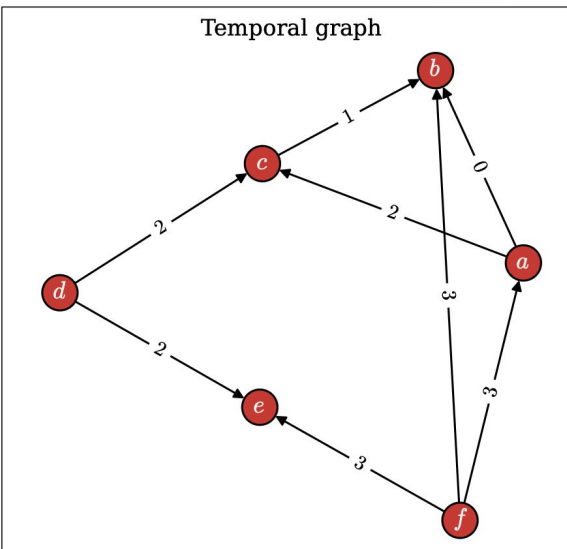
TemporalMultiGraph (t=4) with 32 nodes and 97 edges



3.1. Improve algorithm

Requires: Software infrastructure for temporal graphs

- Open source and freely distributed
- Easy snapshot slicing
- Drawing functions
- Data loaders/generators
- **Transform/Conversion**



3.1. Improve algorithmi

Requires: Software infrastructure for temporal g

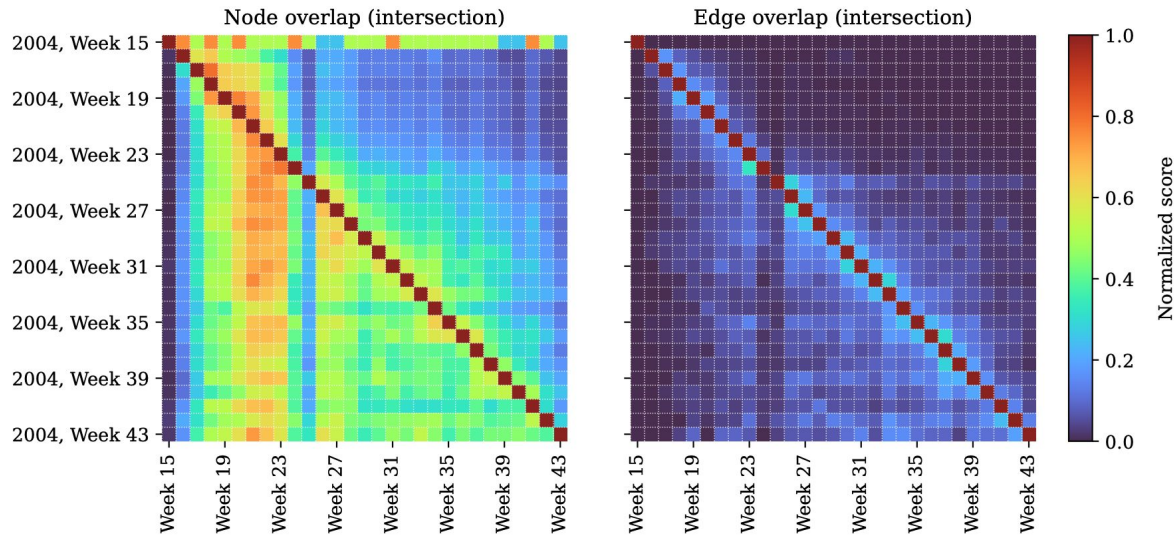
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Format	Parameter (Package)	Calls (Function)
CuGraph	'cugraph'	to_cugraph()
CuPy	'cupy'	to_cupy()
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DyNetX	'dynetx'	to_dynetx()
graph-tool	'graph_tool'	to_graph_tool()
igraph	'igraph'	to_igraph()
NetworkKit	'networkkit'	to_networkkit()
NumPy	'numpy'	to_numpy()
Pandas	'pandas'	to_pandas()
PyTorch Geometric	'torch_geometric'	to_torch_geometric()
SciPy	'scipy'	to_scipy()
SNAP	'snap'	to_snap()
StellarGraph	'stellargraph'	to_stellargraph()
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3.1. Improve algorithmic clustering efficiency

Requires: Software infrastructure for temporal graphs

- Open source and freely distributed (3-clause BSD license), the library includes functions for:
 - Easy snapshot slicing
 - Drawing functions
 - Data loaders/generators
 - Transform/Conversion
 - **Utility functions**



(Weekly node and edge overlap in the CollegeMsg dataset)

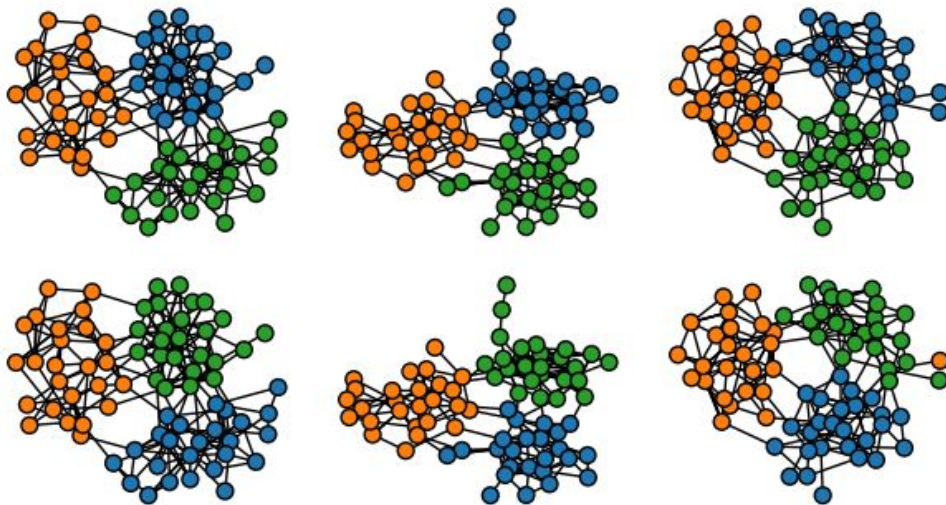
3.1. Improve **algorithmic clustering** efficiency

Requires: Software infrastructure for temporal graphs

- Open source and freely distributed (3-clause BSD license), the library includes functions for:
 - Easy snapshot slicing
 - Drawing functions
 - Data loaders/generators
 - Transform/Conversion
 - Utility functions
 - [Community detection](#) and other algorithms (CPU/GPU)

```
>>> y_pred = tx.spectral_clustering(TG, k=3, operator="laplacian")
```

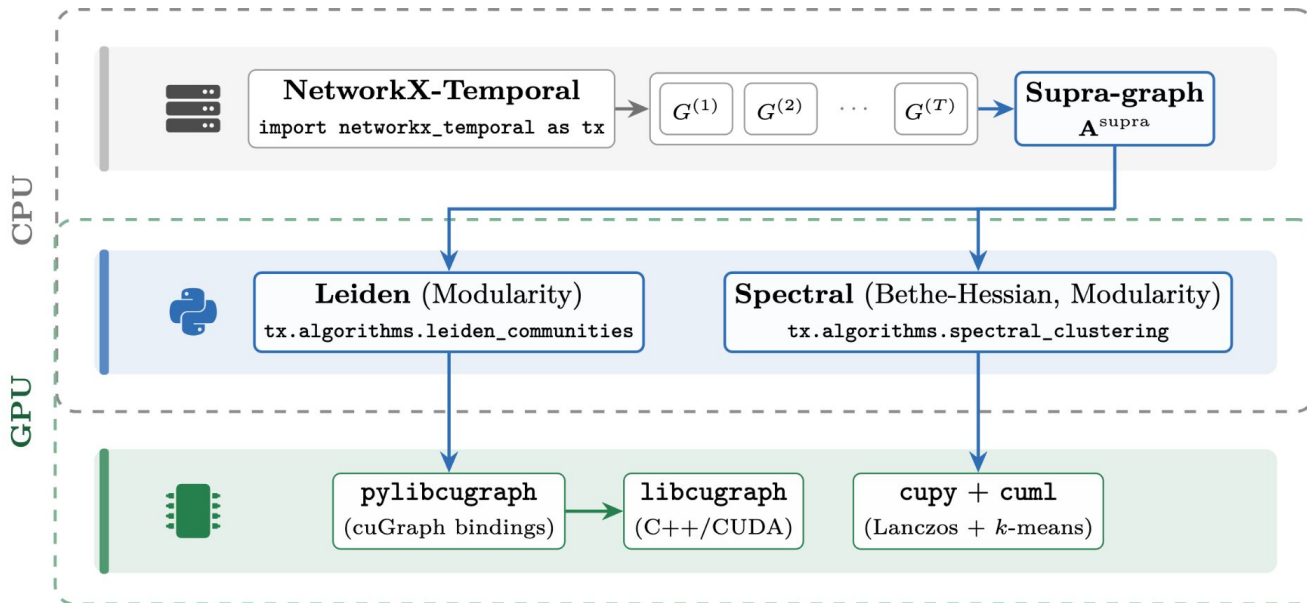
Ground Truths (top) vs. Clustering Results (bottom)



3.1. Improve **algorithmic clustering** efficiency

Requires: Software infrastructure for temporal graphs

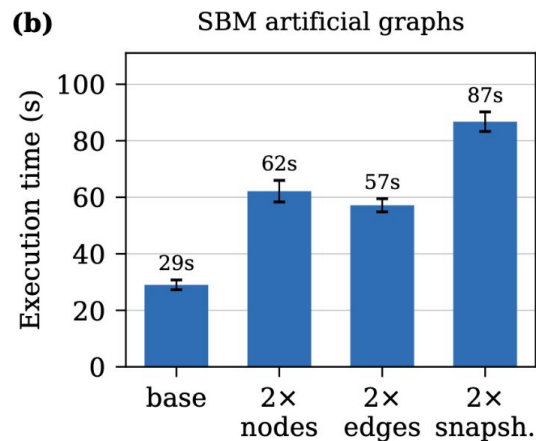
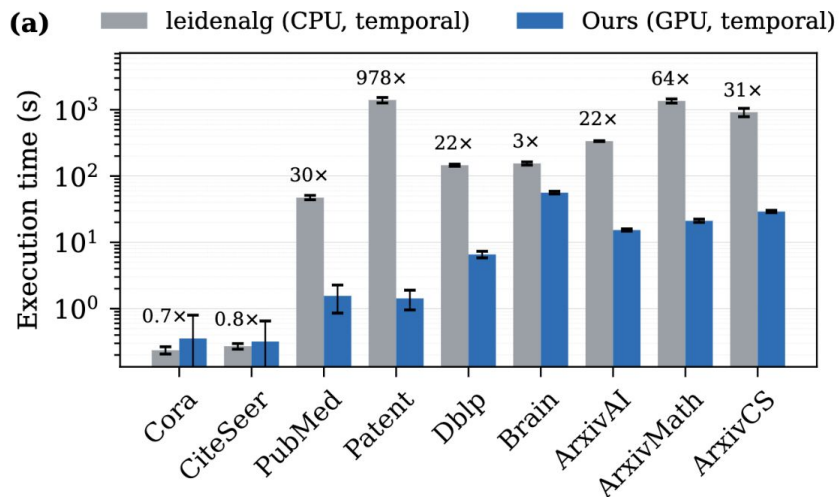
- **Result:** state-of-the-art performance on GPU (both NVIDIA CUDA and AMD ROCm) devices, with *zero-code-change acceleration* by setting an environment var **NX_GPU_AUTOCONFIG=1**.



3.1. Improve **algorithmic clustering** efficiency

Requires: Software infrastructure for temporal graphs

- **Result:** state-of-the-art performance on GPU (both NVIDIA CUDA and AMD ROCm) devices, with *zero-code-change acceleration* by setting an environment var **NX_GPU_AUTOCONFIG=1**.



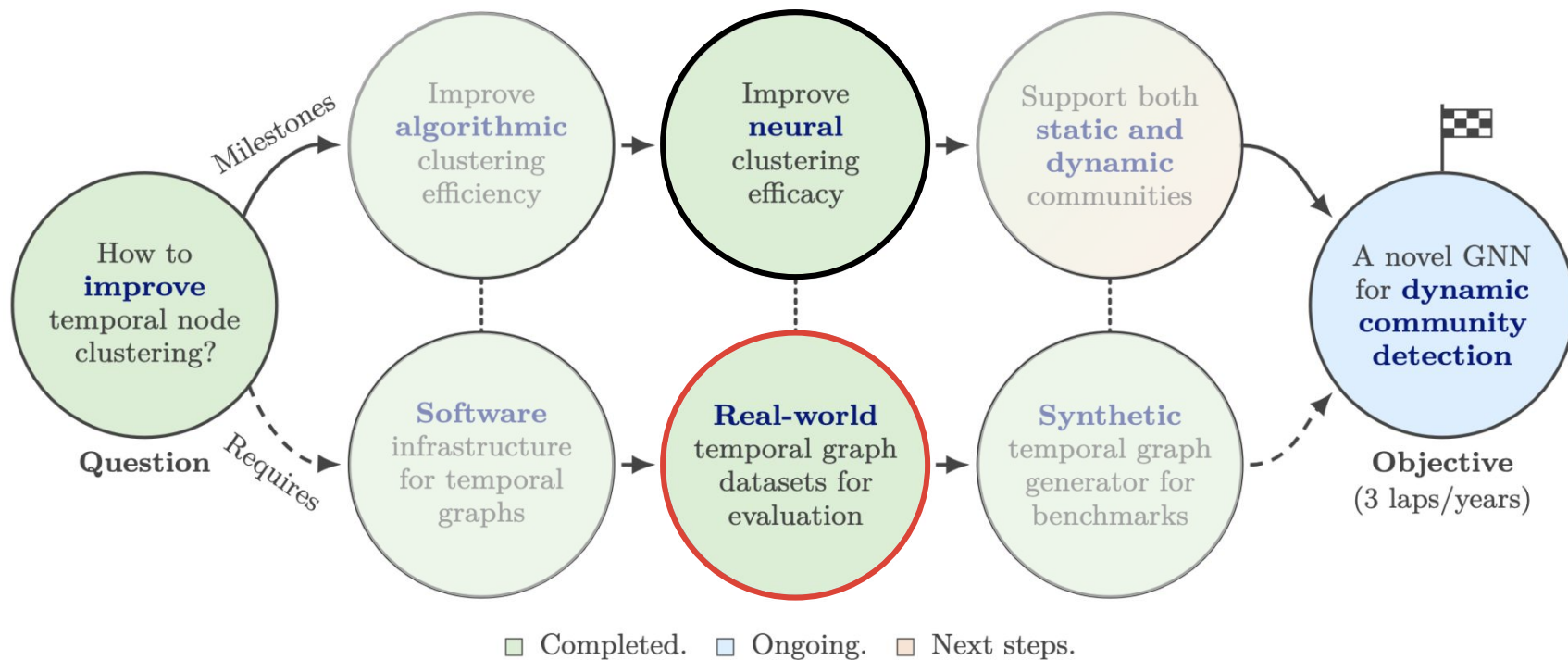
- Speedups of up to ~3 orders of magnitude vs. CPU baselines (Intel Xeon Gold 6330/NVIDIA 100).

Dataset	$ \mathcal{V} $	$\Sigma(\mathcal{V})$	$ \mathcal{E} $	$\Sigma(\mathcal{E})$	$ T $	$ C $
CiteSeer [†] [46]	3 279	3 279	4 552	4 552	1	6
Cora [†] [46]	2 708	2 708	5 278	5 278	1	7
Brain [33]	5 000	60 000	878 207	947 744	12	10
Dblp [49]	28 085	101 797	153 822	222 165	27	10
Patent [14]	12 214	41 529	41 916	41 916	891	6
PubMed [27]	19 717	37 003	44 324	44 324	42	3
School [19]	327	309 006	7 004	188 508	7 375	9
ArxivAI [17]	69 854	142 316	696 819	696 819	27	5
ArxivCS [17]	169 343	374 433	1 157 799	1 157 799	29	40
ArxivLarge [‡] [17]	1 324 064	4 998 391	13 649 351	13 649 351	40	172
ArxivMath [17]	270 013	614 578	783 165	783 165	31	31
SBM [29]	50 000	250 000	1 250 539	1 251 057	5	10
SBM-N [29]	100 000	500 000	2 500 515	2 501 000	5	10
SBM-E [29]	50 000	250 000	2 498 067	2 500 045	5	10
SBM-T [29]	50 000	500 000	2 495 376	2 497 636	10	10

Table 1. Dataset properties. $|\mathcal{V}|$ and $|\mathcal{E}|$ denote unique nodes and edges; $\Sigma(\mathcal{V})$ and $\Sigma(\mathcal{E})$, the sum of nodes and edges over time, i.e., counting each occurrence across snapshots; $|T|$ and $|C|$ are the number of snapshots and communities; [†] marks static graphs used as single-snapshot baselines; and [‡], the largest dataset, where a single CPU run allowed to exceed the time budget completed in ≈ 6 h, versus ≈ 10 min on GPU [24].

3.2. Improve neural clustering efficacy

Requires: Real-world temporal graph datasets for evaluation

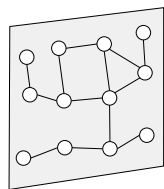
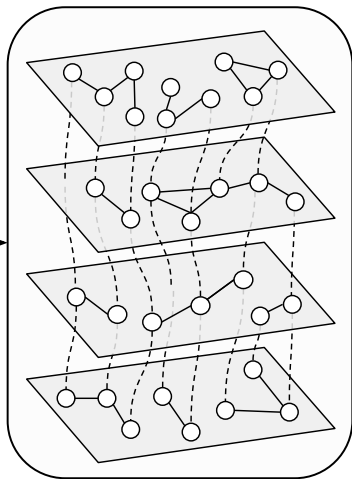


3.2.

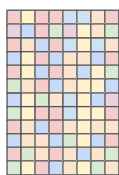
Requires

INPUT

(continuous-time temporal graph)



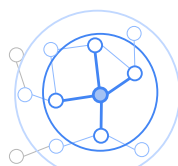
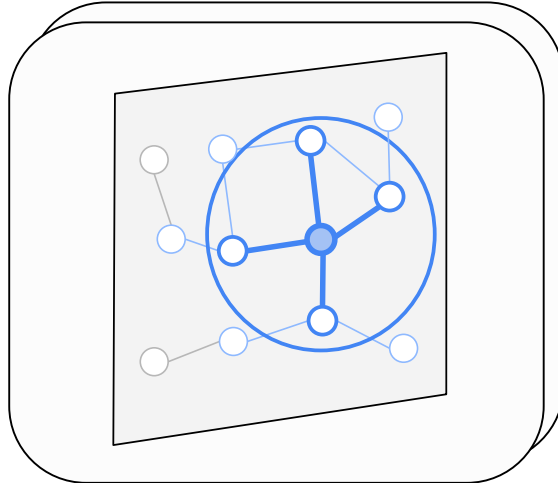
$f_h(\tilde{\mathbf{A}})$



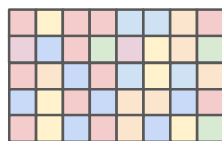
$\mathbf{X}$

HIDDEN LAYER(S)

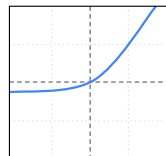
(any optionally multilayer graph encoder)



$N(u)$



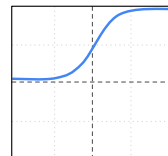
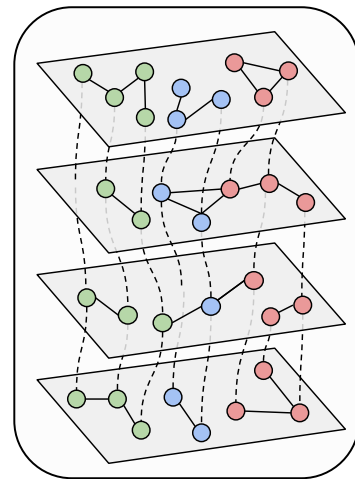
$\mathbf{X}[N(u)]$



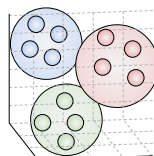
SeLU

OUTPUT

(community assignments)



Softmax



$\mathbf{C}$

$$\mathcal{L}_{\text{LMoN}} = \underbrace{-Q + S + \mathcal{R}}_{\text{Modularity Sm.+Reg.}} + \underbrace{\mathcal{H}}_{\text{Hawkes NLL}}$$

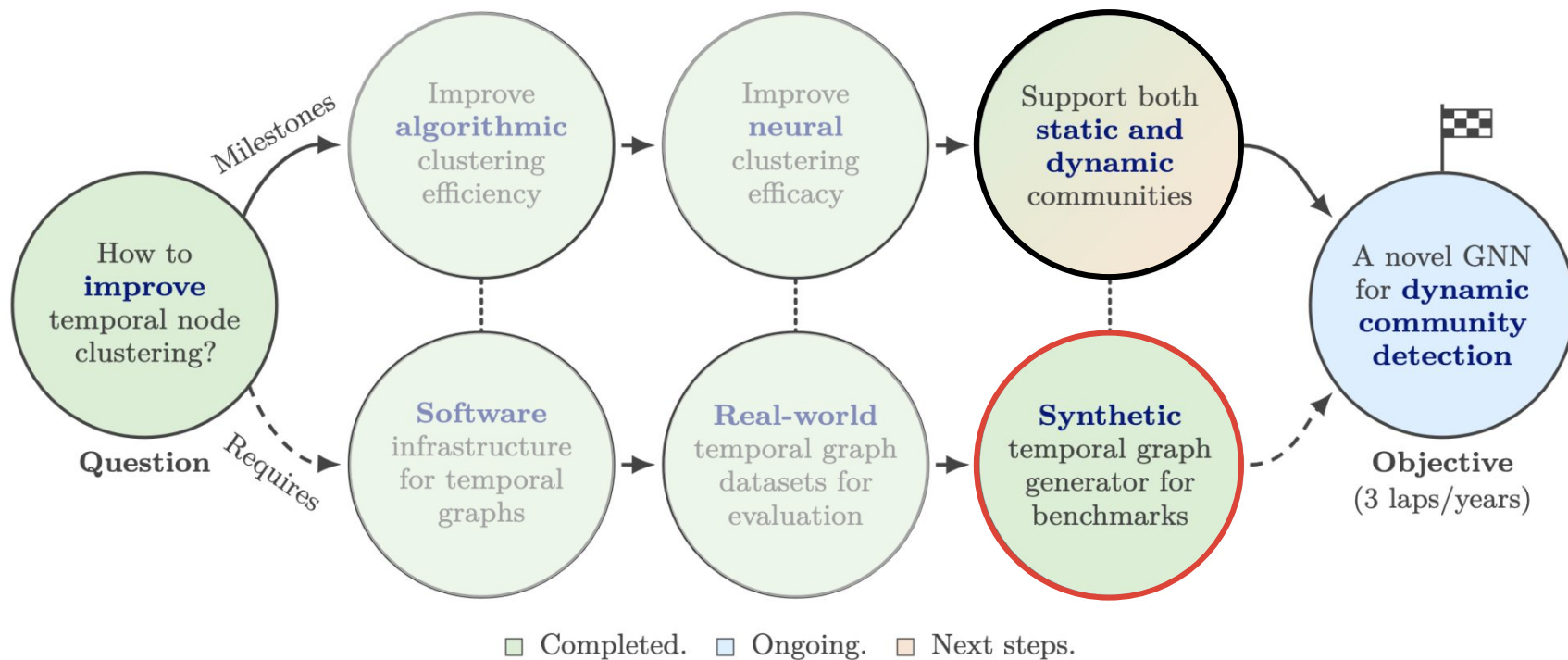
3.2. Improve neural clustering efficacy

Requires: Real-world temporal graph datasets for evaluation

- Most **real-world** systems have **attributes** at node/edge levels $\rightarrow$ leading to neural approaches.
- We introduce 🍌 **LMoN** – an *encoder-agnostic* Longitudinal Modularity optimization Network.
- Our model builds upon a SOTA model while maintaining its best-in-class scalability $O(d^2n+m)$:
 - **Objective:** a novel spectral relaxation (*continuous values*) of *longitudinal modularity*.
 - **Operator:** a Hawkes-Laplacian mechanism that *learns* how to reweight the graph.
- **Result:** *end-to-end differentiable* community detection on **attributed temporal** graphs.
- However, **two main issues** compound temporal graph clustering in **real-world** applications.

3.3. Support static and dynamic communities

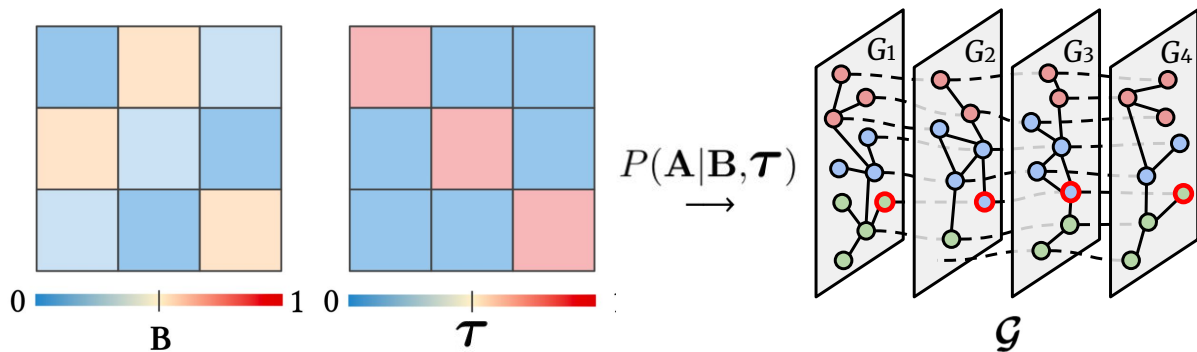
Requires: Synthetic temporal graph generator for benchmarks



3.3. Support static and dynamic communities

Requires: Synthetic temporal graph generator for benchmarks

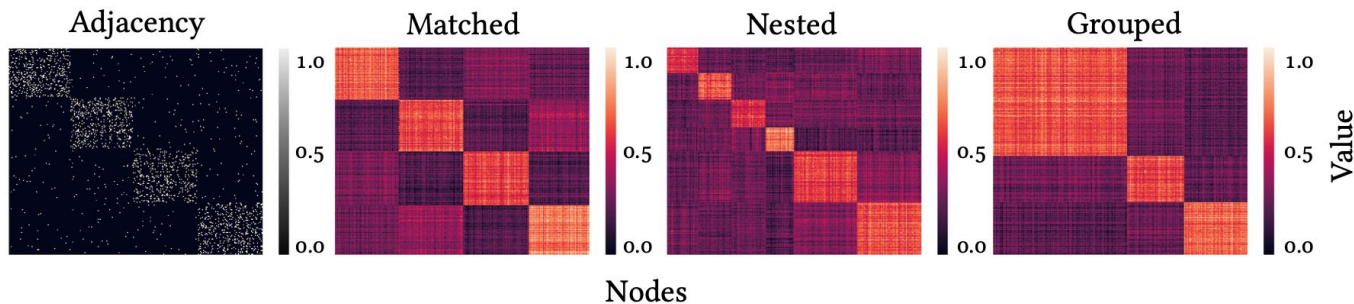
- However, **two main issues** compound temporal graph clustering in real-world applications.
 - **Real-world data is messy:** there is no guarantee of attribute and topological alignment.
 - **The ground truths (clusters)** themselves may not be aligned with the graph topology/attr.
- Solution: a *principled* benchmarking framework to compare and evaluate clustering models...



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Requires: Synthetic temporal graph generator for benchmarks

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- ...that generates graphs with *known ground truths* and *community-aligned topology and attributes*.



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Requires: Synthetic temporal graph generator for benchmarks

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 - **Real-world data is messy: there is no guarantee of attribute and topological alignment.**
 - **The ground truths (clusters) themselves may not be aligned with the graph topology/attr.**
 - Solution: a *principled* benchmarking framework to compare and evaluate clustering models...
 - ...that generates graphs with *known ground truths* and *community-aligned topology and attributes*.
 - **Result:** we can evaluate exactly *when and under which conditions* **neural** > **algorithm** methods.
- Our evaluation revealed: in some real-world applications, **algorithms still outperform GNNs!**

4. Future work

Where do we go from here?

- Two publications “in the oven” on temporal community detection (1 algorithmic, 1 neural method).
- A new research direction for **causal learning** at using *principled pooling primitives* for learning on graphs.
- Our code is available and **production-ready** at networkx-temporal.org (with documentation + examples).
- Questions and feedback appreciated!
Thank you for your attention :-)



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Toward Efficient Community Detection on Time-Varying Attributed Graphs



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